

Numerical study of multiparticle probabilities in $\lambda\phi^4$ theory

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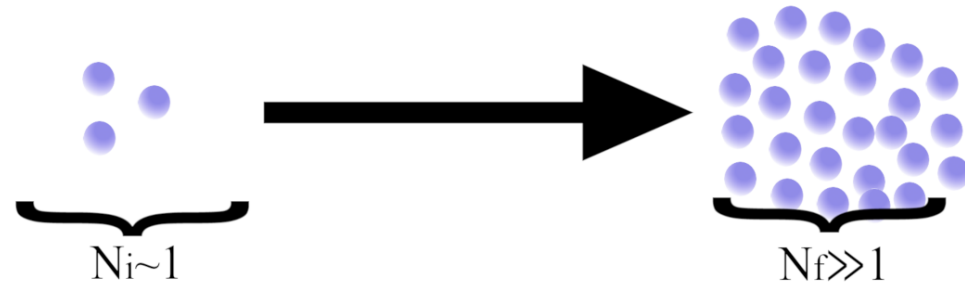
Overview

- ◆ Subject of research
- ◆ Research
- ◆ Future aims
- ◆ Q&A section

Multiparticle scattering

Multiparticle scattering: $N \rightarrow \infty, A_{\text{tree}} \sim N! \lambda^{\frac{n}{2}}$

Multiparticle creation:



If it is unsuppressed, it will
introduce energy cutoff scale

Considered theory: $S = \frac{4\pi}{\lambda} \int dr' dt' \left[\frac{1}{2} \left(\frac{\partial \phi}{\partial t'} \right)^2 - \frac{1}{2} \left(\frac{\partial \phi}{\partial r'} \right)^2 - \frac{\phi^2}{2} - \frac{\phi^4}{4r'^2} \right]$

$$r' = mr, t' = mt, \lambda \rightarrow 0, \frac{\lambda N}{4\pi} = \tilde{N}, \frac{\lambda E}{4\pi} = \tilde{E}$$

Semiclassical approach

Path integral:

$$\langle f|i \rangle = \int_{\varphi_i}^{\varphi_f} \mathcal{D}\varphi e^{iS[\varphi]}$$

$$|i \rangle = e^{\frac{4\pi j}{\sqrt{\lambda}} \int dr r f(r) \varphi(0,r)} |0 \rangle; \quad \langle f| = \sum_a \langle a | \hat{P}_E \hat{P}_{N_f}$$

Conditions for semiclassics:

$$S \sim \frac{1}{\lambda}, \quad \lambda \rightarrow 0$$

Expansion near the saddle-point:

$$S[\varphi] = S[\varphi_{saddle}] + S''[\varphi_{saddle}](\delta\varphi)^2 + \dots$$

Saddle-point equations

Equations:

$$\frac{\partial^2 \varphi}{\partial t^2} - \frac{\partial^2 \varphi}{\partial r^2} + \varphi + \frac{\varphi^3}{r^2} = -i j r f(r) \delta(t)$$

Boundary conditions:

$$\varphi(t, k) = \frac{1}{\sqrt{2\omega_k}} (f_k e^{-i\omega_k t + ikr} + g_k^\dagger e^{i\omega_k t - ikr})$$

$$i : f_k = 0$$

$$f : f_k = e^{-\theta + 2T\omega_k} g_k$$

Probability in main exponential order:

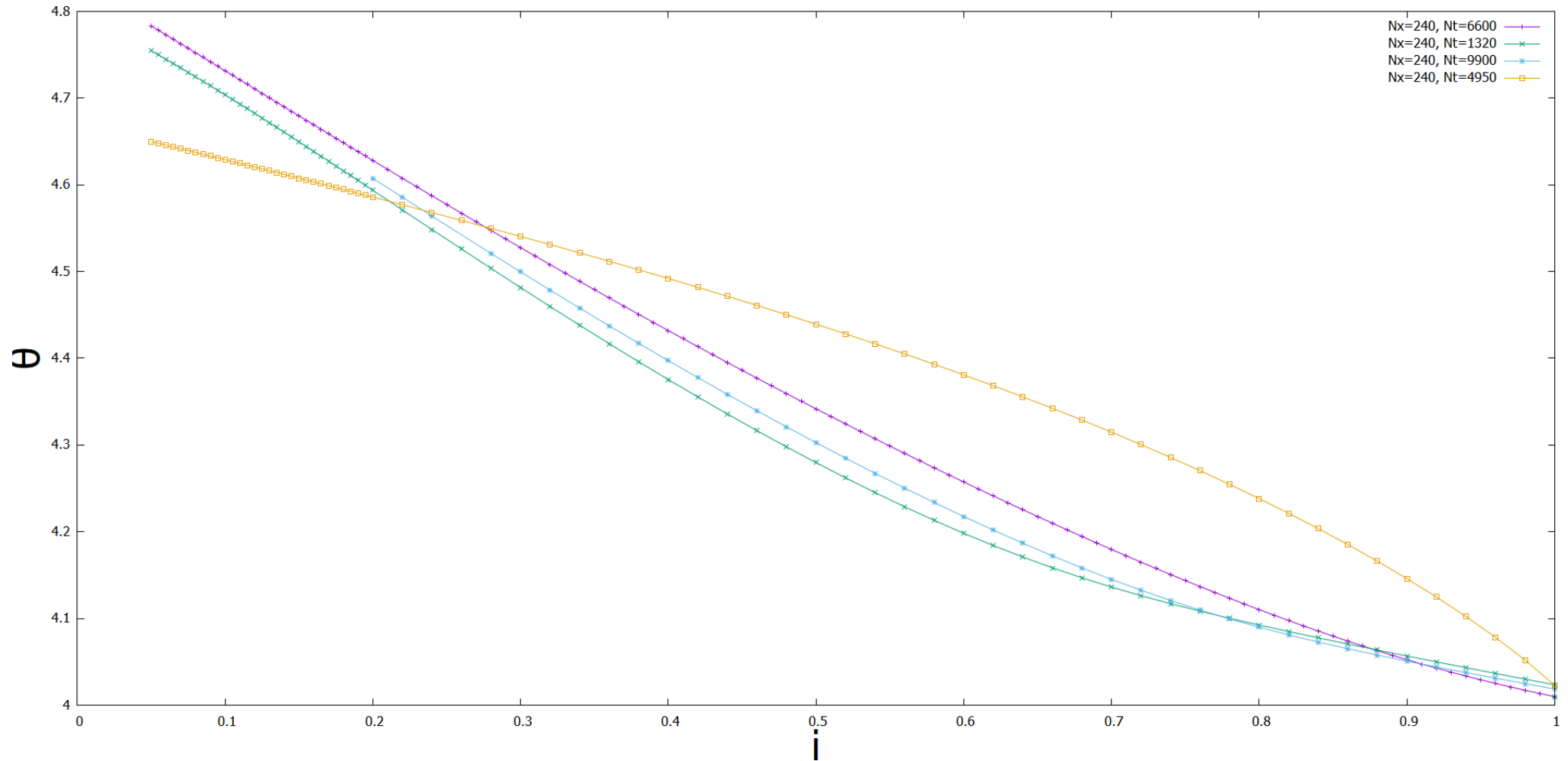
$$P \sim e^W$$

$$W = 2ET - N_f \theta - 2ImS + Im \int dr \varphi \frac{\partial \varphi}{\partial t} \Big|_{t=t_f}$$

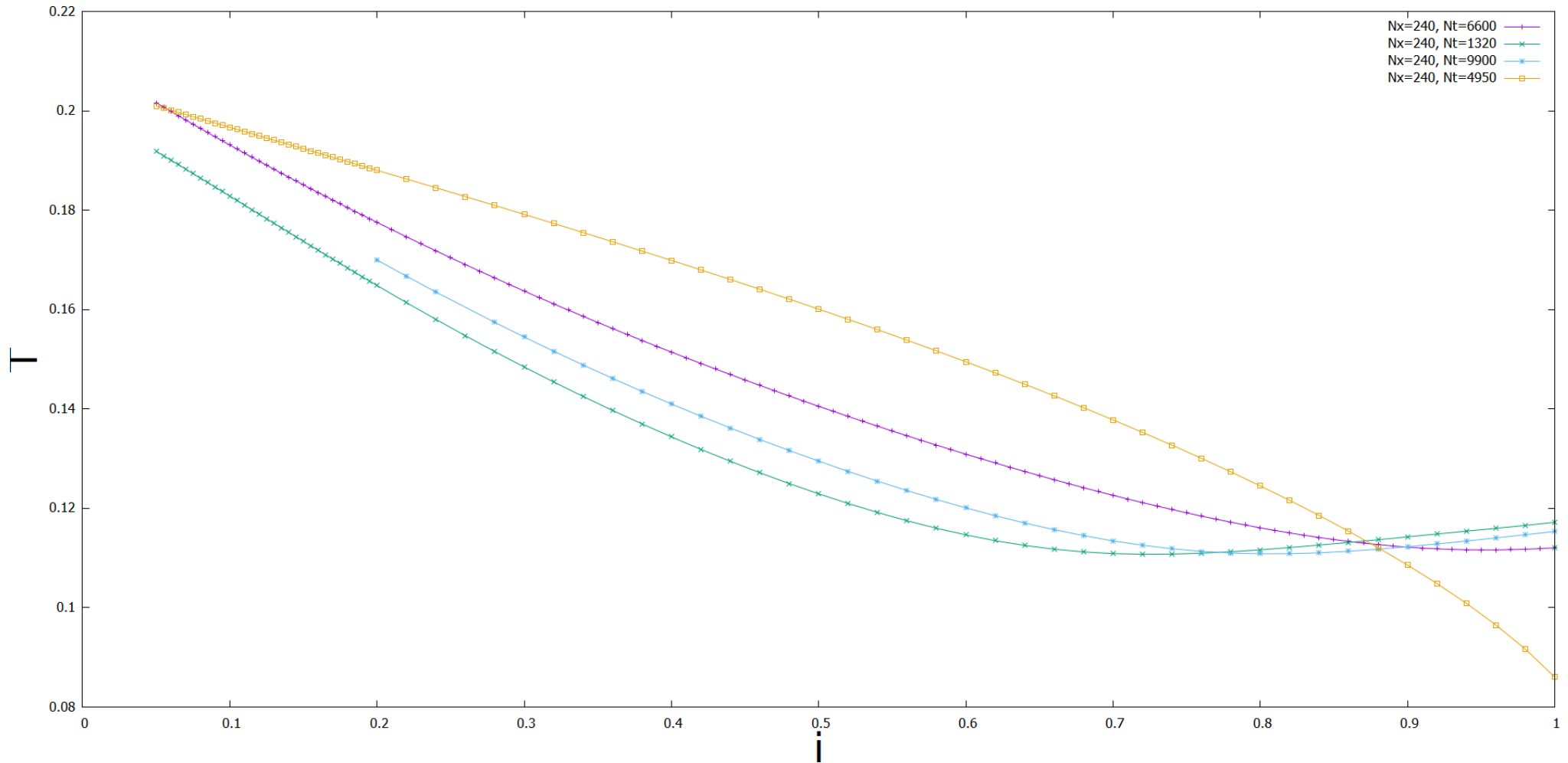
Numerical realisation

- ◆ Take the first approximation from a source-dominated theory
- ◆ Use Newton-Raphson scheme to converge to the theory with self-interaction
- ◆ Take a limit $j \rightarrow 0$ for different fixed E, N_f or T, θ

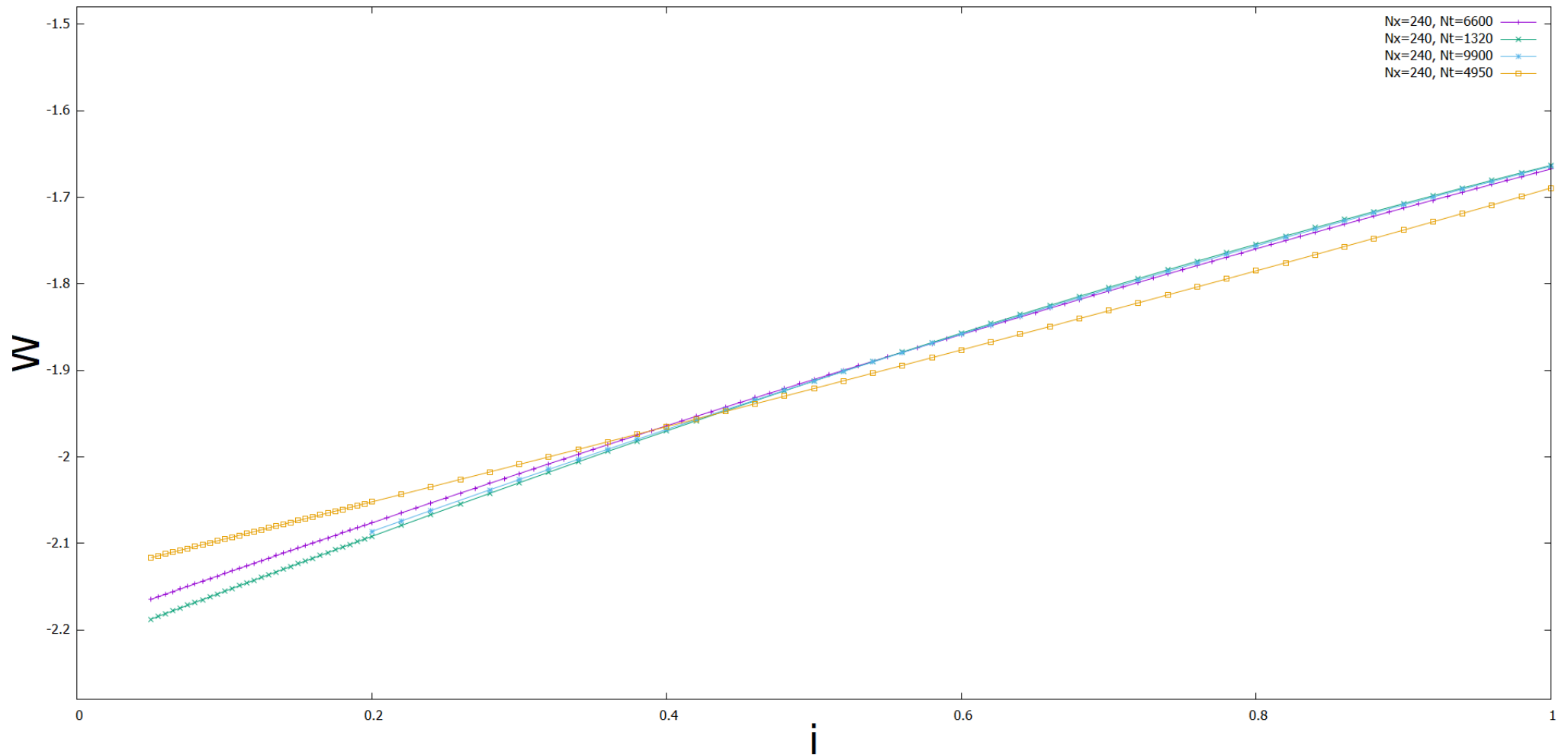
Limit $j \rightarrow 0$ for E, N_{out} fixed



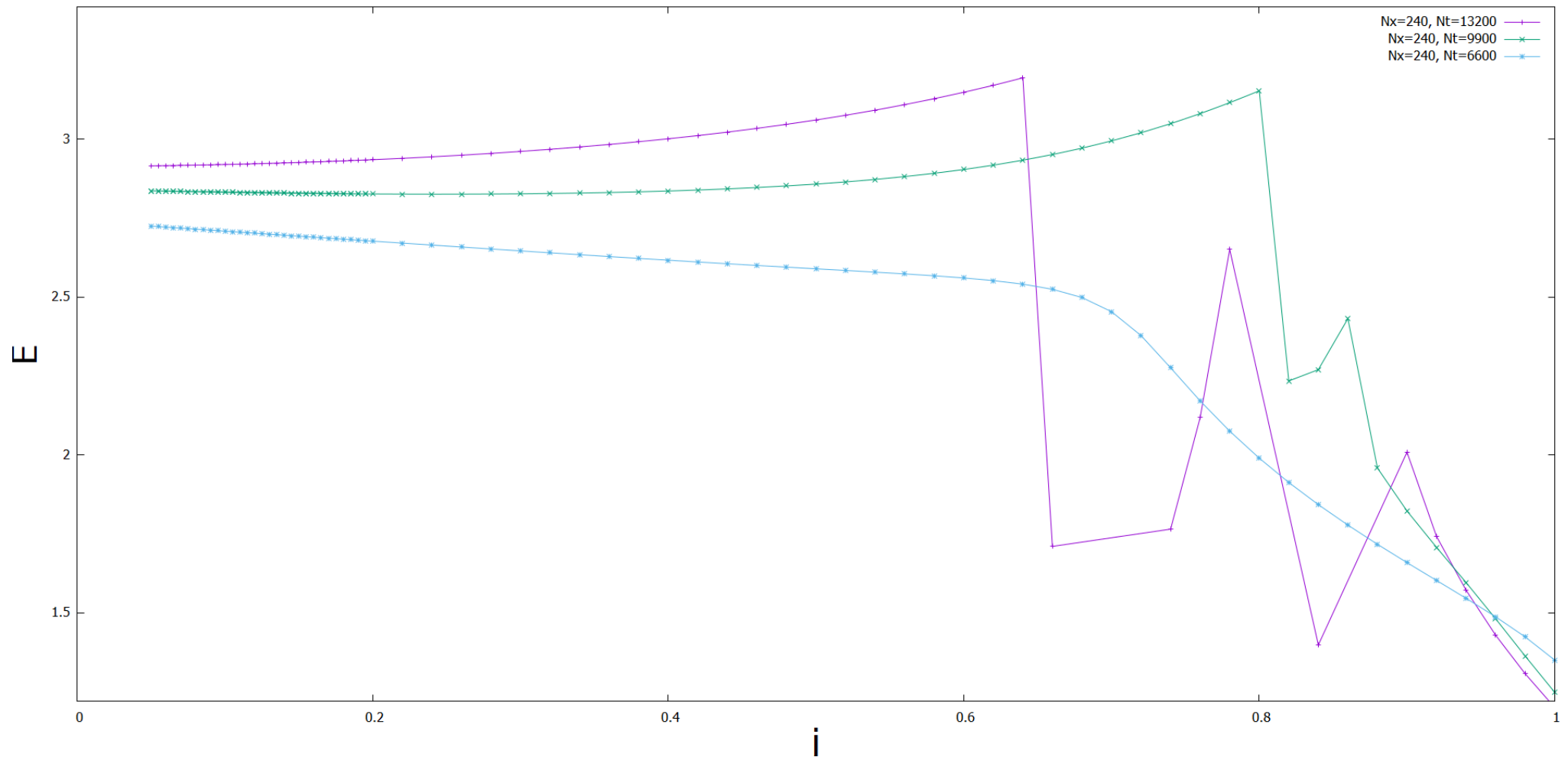
Limit $j \rightarrow 0$ for E, N_{out} fixed



Limit $j \rightarrow 0$ for E, N_{out} fixed



Limit $j \rightarrow 0$ for T, θ fixed



What should be done next

- ♦ Analytically find saddle-point solutions when $j \rightarrow 0$ in regimes which allow it
- ♦ Find dependence of $E, N_f, (T, \theta), W$ on j
- ♦ Consider broken φ^4 theory

Any questions?